

**Zbl 014.01104**

**Erdős, Pál**

*A generalization of a theorem of Besicovitch.* (In English)

**J. London Math. Soc. 11, 92-98 (1936).**

Let  $\delta_a$  denote the density of the set consisting of all numbers which have a divisor between  $a$  and  $2a$ . It was proved by *A.S.Besicovitch* (see Zbl 009.39504) that  $\liminf_{a \rightarrow \infty} \delta_a = 0$ . Let  $d_a$  denote the density of the set consisting of all numbers which have a divisor between  $a$  and  $a^{1+\varepsilon_a}$ . The author proves that if  $\varepsilon \rightarrow 0$  as  $a \rightarrow \infty$  then  $d_a \rightarrow 0$ . This is easily seen to be the best possible result of its kind. It is impossible to give a sketch of the highly ingenious proof within the limits of a review.

*Davenport (Cambridge)*

Classification:

11N25 Distribution of integers with specified multiplicative constraints