Research Article

(λ, μ) -Fuzzy Version of Ideals, Interior Ideals, Quasi-Ideals, and Bi-Ideals

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We introduced (λ, μ) -fuzzy ideals, (λ, μ) -fuzzy interior ideals, (λ, μ) -fuzzy quasi-ideals, and (λ, μ) -fuzzy bi-ideals of an ordered semigroup and studied them. When $\lambda = 0$ and $\mu = 1$, we meet the ordinary fuzzy ones. This paper can be seen as a generalization of Kehayopulu and Tsingelis (2006), Kehayopulu and Tsingelis (2007), and Yao (2009).

1. Introduction and Preliminaries

An ideal of a semigroup is a special subsemigroup satisfying certain conditions. The best way to know an algebraic structure is to begin with a special substructure of it. There are plenty of papers on ideals. After Zadeh' introduction of fuzzy set in 1965 (see [1]), the fuzzy sets have been used in the reconsideration of classical mathematics. Also, fuzzy ideals have been considered by many researchers. For example, Kim [2] studied intuitionistic fuzzy ideals of semigroups, Meng and Guo [3] researched fuzzy ideals of BCK/BCI-algebras, Koguep [4] researched fuzzy ideals of hyperlattices, and Kehayopulu and Tsingelis [5] researched fuzzy interior ideals of ordered semigroups.

Recently, Yuan et al. [6] introduced the concept of fuzzy subfield with thresholds. A fuzzy subfield with thresholds λ and μ is also called a (λ , μ)-fuzzy subfield. Yao continued to research (λ , μ)-fuzzy normal subfields, (λ , μ)-fuzzy quotient subfields, (λ , μ)-fuzzy subrings, and (λ , μ)-fuzzy ideals in [7–10]. Feng et al. researched (λ , μ)-fuzzy sublattices and (λ , μ)-fuzzy subhyperlattices in [11].

An ordered semigroup (S, \circ, \leq) is a poset (S, \leq) equipped with a binary operation \circ , such that

- (1) (S, \circ) is a semigroup, and
- (2) if $x, a, b \in S$, then

$$a \le b \Rightarrow \begin{cases} a \circ x \le b \circ x \\ x \circ a \le x \circ b. \end{cases}$$
(1.1)

Given an ordered semigroup *S*, a fuzzy subset of *S* (or a fuzzy set in *S*) is an arbitrary mapping $f : S \rightarrow [0,1]$, where [0,1] is the usual closed interval of real numbers. For any $\alpha \in [0,1]$, f_{α} is defined by $f_{\alpha} = \{x \in S | f(x) \ge \alpha\}$. For $a \in S$, we define that $A_{\alpha} = \{(y,z) \in S \times S | a \le yz\}$. For two fuzzy subsets *f* and *g* of *S*, we define the multiplication of *f* and *g* as the fuzzy subset of *S* defined by

$$(f * g)(a) = \begin{cases} \sup_{(y,z) \in A_a} (f(y) \wedge g(z)), & \text{if } A_a \neq \emptyset, \\ (y,z) \in A_a & 0, \\ 0, & \text{if } A_a = \emptyset. \end{cases}$$
(1.2)

In the set of fuzzy subsets of *S*, we define the order relation as follows: $f \subseteq g$ if and only if $f(x) \leq g(x)$ for all $x \in S$. For two fuzzy subsets *f* and *g* of *S*, we define

$$(f \cap g)(x) = f(x) \wedge g(x), \qquad (f \cup g)(x) = f(x) \vee g(x). \tag{1.3}$$

Note that we use $a \land b$ to denote min(a, b) and use $a \lor b$ to denote max(a, b).

For any $\alpha \in [0,1]$, α can be seen as a fuzzy subset of *S* which is defined by $\alpha(x) = \alpha$, for all $x \in S$.

In the following, we will use *S* or (S, \circ, \leq) to denote an ordered semigroup and the multiplication of *x*, *y* will be *xy* instead of $x \circ y$.

In the rest of this paper, we will always assume that $0 \le \lambda < \mu \le 1$.

In this paper, we introduced (λ, μ) -fuzzy ideals, (λ, μ) -fuzzy interior ideals, (λ, μ) -fuzzy quasi-ideals and (λ, μ) -fuzzy bi-ideals of an ordered semigroup. We obtained the followings:

- (1) in an ordered semigroup, every (λ, μ) -fuzzy ideal is a (λ, μ) -fuzzy interior ideal;
- (2) in an ordered semigroup, every (λ, μ) -fuzzy right (resp. left) ideal is a (λ, μ) -fuzzy quasi-ideal;
- (3) in an ordered semigroup, every (λ, μ) -fuzzy quasi-ideal is a (λ, μ) -fuzzy bi-ideal;
- (4) in a regular ordered semigroup, the (λ, μ) -fuzzy quasi-ideals and the (λ, μ) -fuzzy bi-ideals coincide.

2. (λ, μ) -Fuzzy Ideals and (λ, μ) -Fuzzy Interior Ideals

Definition 2.1. Let (S, \cdot, \leq) be an ordered semigroup. A fuzzy subset f of S is called a (λ, μ) -*fuzzy right ideal* (resp. (λ, μ) -*fuzzy left ideal*) of S if

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- (1) $f(xy) \lor \lambda \ge f(x) \land \mu$ (resp. $f(xy) \lor \lambda \ge f(y) \land \mu$) for all $x, y \in S$, and
- (2) if $x \le y$, then $f(x) \lor \lambda \ge f(y) \land \mu$ for all $x, y \in S$.

A fuzzy subset *f* of *S* is called a (λ, μ) -fuzzy ideal of *S* if it is both a (λ, μ) -fuzzy right and a (λ, μ) -fuzzy left ideal of *S*.

Example 2.2. Let $(S, *, \le)$ be an ordered semigroup where $S = \{e, a, b\}$ and $e \le a \le b$. The multiplication table is defined by the following:

A fuzzy set *f* is defined as follows:

$$\frac{S}{f} = \frac{e}{0.1} \frac{a}{0.2} \frac{b}{0.3}$$
(2.2)

Then, *f* is a (0.3, 0.7)-fuzzy ideal of *S*. But it is not a fuzzy ideal of *S*.

Definition 2.3 (see [12]). If (S, \circ, \leq) is an ordered semigroup, a nonempty subset *A* of *S* is called an interior ideal of *S* if

- (1) $SAS \subseteq A$, and
- (2) if $a \in A, b \in S$, and $b \le a$, then $b \in A$.

Definition 2.4. If (S, \circ, \leq) is an ordered semigroup, a fuzzy subset f of S is called a (λ, μ) -fuzzy interior ideal of S if

- (1) $f(xay) \lor \lambda \ge f(a) \land \mu$ for all $x, a, y \in S$, and
- (2) if $x \le y$, then $f(x) \lor \lambda \ge f(y) \land \mu$.

In the previous example, f is also a (0.3, 0.7)-fuzzy interior ideal of S. In fact, every fuzzy ideal of an ordered semigroup is a fuzzy interior.

Theorem 2.5. Let (S, \circ, \leq) be an ordered semigroup and f a (λ, μ) -fuzzy ideal of S, then f is a (λ, μ) -fuzzy interior ideal of S.

Proof. Let $x, a, y \in S$. Since f is a (λ, μ) -fuzzy left ideal of S and $x, ay \in S$, we have

$$f(x(ay)) \lor \lambda \ge f(ay) \land \mu.$$
(2.3)

Since *f* is a (λ, μ) -fuzzy right ideal of *S*, we have

$$f(ay) \lor \lambda \ge f(a) \land \mu. \tag{2.4}$$

From (2.3) and (2.4) we know that $f(xay) \lor \lambda = (f(x(ay)) \lor \lambda) \lor \lambda \ge (f(ay) \land \mu) \lor \lambda = (f(ay) \lor \lambda) \land (\mu \lor \lambda) \ge f(a) \land \mu$.

Theorem 2.6. Let (S, \circ, \leq) be an ordered semigroup, then f is a (λ, μ) -fuzzy interior ideal of S if and only if f_{α} is an interior ideal of S for all $\alpha \in (\lambda, \mu]$.

Proof. Let *f* be a (λ, μ) -fuzzy interior ideal of *S* and $\alpha \in (\lambda, \mu]$.

First of all, we need to show that $xay \in f_{\alpha}$, for all $a \in f_{\alpha}$, $x, y \in S$.

From $f(xay) \lor \lambda \ge f(a) \land \mu \ge \alpha \land \mu = \alpha$ and $\lambda < \alpha$, we conclude that $f(xay) \ge \alpha$, that is, $xay \in f_{\alpha}$.

Then, we need to show that $b \in f_{\alpha}$ for all $a \in f_{\alpha}$, $b \in S$ such that $b \leq a$.

From $b \le a$ we know that $f(b) \lor \lambda \ge f(a) \land \mu$ and from $a \in f_{\alpha}$ we have $f(a) \ge \alpha$. Thus, $f(b) \lor \lambda \ge \alpha \land \mu = \alpha$. Notice that $\lambda < \alpha$, then we conclude that $f(b) \ge \alpha$, that is, $b \in f_{\alpha}$.

Conversely, let f_{α} be an interior ideal of *S* for all $\alpha \in (\lambda, \mu]$.

If there are $x_0, a_0, y_0 \in S$, such that $f(x_0a_0y_0) \lor \lambda < \alpha = f(a_0) \land \mu$, then $\alpha \in (\lambda, \mu]$, $f(a_0) \ge \alpha$ and $f(x_0a_0y_0) < \alpha$. That is $a_0 \in f_\alpha$ and $x_0a_0y_0 \notin f_\alpha$. This is a contradiction with that f_α is an interior ideal of *S*. Hence $f(xay) \lor \lambda \ge f(a) \land \mu$ holds for all $x, a, y \in S$.

If there are $x_0, y_0 \in S$ such that $x_0 \leq y_0$ and $f(x_0) \lor \lambda < \alpha = f(y_0) \land \mu$, then $\alpha \in (\lambda, \mu], f(y_0) \geq \alpha$, and $f(x_0) < \alpha$, that is, $y_0 \in f_\alpha$ and $x_0 \notin f_\alpha$. This is a contradiction with that f_α is an interior ideal of *S*. Hence if $x \leq y$, then $f(x) \lor \lambda \geq f(y) \land \mu$.

3. (λ, μ) -Fuzzy Quasi-Ideals and (λ, μ) -Fuzzy Bi-Ideals

Definition 3.1. Let (S, \circ, \leq) be an ordered semigroup. A subset *A* of *S* is called a quasi-ideal of *S* if

(1) $AS \cap SA \subseteq S$, and

(2) if $x \in S$ and $x \leq y \in A$, then $x \in A$.

Definition 3.2. A nonempty subset A of an ordered semigroup S is called a bi-ideal of S if it satisfies

- (1) $ASA \subseteq A$, and
- (2) $x \in S$ and $x \leq y \in A$, then $x \in A$.

Definition 3.3. Let (S, \circ, \leq) be an ordered semigroup. A fuzzy subset f of S is called a (λ, μ) -fuzzy quasi-ideal of S if

- (1) $f \cup \lambda \supseteq (f * 1) \cap (1 * f) \cap \mu$, and
- (2) if $x \le y$, then $f(x) \lor \lambda \ge f(y) \land \mu$ for all $x, y \in S$.

Definition 3.4. Let (S, \circ, \leq) be an ordered semigroup. A fuzzy subset f of S is called a (λ, μ) -fuzzy bi-ideal of S if for all $x, y, z \in S$,

- (1) $f(xyz) \lor \lambda \ge (f(x) \land f(z)) \land \mu$, and
- (2) if $x \le y$, then $f(x) \lor \lambda \ge f(y) \land \mu$.

Remark 3.5. It is easy to see that a fuzzy quasi-ideal [13] of *S* is a (0, 1)-fuzzy quasi-ideal of *S*, and a fuzzy bi-ideal [13] of *S* is a (0, 1)-fuzzy bi-ideal of *S*.

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Theorem 3.6. Let (S, \circ, \leq) be an ordered semigroup, then f is a (λ, μ) -fuzzy quasi-ideal of S if and only if f_{α} is a quasi-ideal of S for all $\alpha \in (\lambda, \mu]$.

Proof. Let *f* be a (λ, μ) -fuzzy quasi-ideal of *S* and $\alpha \in (\lambda, \mu]$. First of all, we need to show that $Sf_{\alpha} \cap f_{\alpha}S \subseteq f_{\alpha}$. If $x \in Sf_{\alpha} \cap f_{\alpha}S$, then $x = st_1 = t_2s$ for some $t_1, t_2 \in f_{\alpha}$ and $s \in S$. From $f \cup \lambda \supseteq (f * 1) \cap (1 * f) \cap \mu$, we conclude that $f(x) \lor \lambda \ge (f * 1)(x) \land (f * 1)(x) \land \mu \ge 0$ $f(t_1) \wedge f(t_2) \wedge \mu \geq \alpha \wedge \mu = \alpha$. Thus, $f(x) \geq \alpha$, and so $x \in f_{\alpha}$. Hence, $S * f_{\alpha} \cap f_{\alpha} * S \subseteq f_{\alpha}$. Next, we need to show that $b \in f_{\alpha}$ for all $a \in f_{\alpha}$, $b \in S$ such that $b \leq a$. From $b \le a$ we know that $f(b) \lor \lambda \ge f(a) \land \mu$ and from $a \in f_{\alpha}$ we have $f(a) \ge \alpha$. Thus, $f(b) \lor \lambda \ge \alpha \land \mu = \alpha$. Notice that $\lambda < \alpha$, we conclude that $f(b) \ge \alpha$, that is, $b \in f_{\alpha}$. Conversely, let f_{α} be a quasi-ideal of *S* for all $\alpha \in (\lambda, \mu]$. Then, $f_{\alpha}S \cap Sf_{\alpha} \subseteq f_{\alpha}$. If there is $x_0 \in S$, such that $f(x_0) \lor \lambda < \alpha = (f * 1)(x) \land (1 * f)(x) \land \mu$, then $\alpha \in S$ $(\lambda,\mu], f(x_0) < \alpha, (f*1)(x_0) \ge \alpha$ and $(1*f)(x_0) \ge \alpha$. That is $x_0 \notin f_\alpha, \sup_{x_0 \le x_1, x_2} f(x_1) \ge \alpha$ and $\sup_{x_0 < x_1 x_2} f(x_2) \ge \alpha.$ From $f_{\alpha}S \cap Sf_{\alpha} \subseteq f_{\alpha}$ and $x_0 \notin f_{\alpha}$, we obtain that $x_0 \notin f_{\alpha}S \cap Sf_{\alpha}$. From $\sup_{x_0 \le x_1 x_2} f(x_1) \ge \alpha$ and $\alpha \ne 0$, we know that there exists at least one pair $(x_1, x_2) \in$ $S \times S$ such that $x_0 \leq x_1 x_2$ and $f(x_1) \geq \alpha$. Thus, $x_0 \leq x_1 x_2 \in f_\alpha S$. Hence, $x_0 \in f_\alpha S$. Similarly, we can prove that $x_0 \in Sf_{\alpha}$. So $x_0 \in f_{\alpha}S \cap Sf_{\alpha}$. This is a contradiction. Hence, $f \cup \lambda \supseteq (f * 1) \cap (1 * f) \cap \mu$ holds. If there are $x_0, y_0 \in S$ such that $x_0 \leq y_0$ and $f(x_0) \lor \lambda < \alpha = f(y_0) \land \mu$, then $\alpha \in f(y_0)$ $(\lambda, \mu], f(y_0) \ge \alpha$ and $f(x_0) < \alpha$, that is, $y_0 \in f_\alpha$ and $x_0 \notin f_\alpha$. This is a contradiction with that f_{α} is a quasi-ideal of *S*. Hence if $x \leq y$, then $f(x) \lor \lambda \geq f(y) \land \mu$.

Theorem 3.7. Let (S, \circ, \leq) be an ordered semigroup, then f is a (λ, μ) -fuzzy bi-ideal of S if and only if f_{α} is a bi-ideal of S for all $\alpha \in (\lambda, \mu]$.

Proof. The proof of this theorem is similar to the proof of the previous theorem. \Box

Theorem 3.8. Let (S, \circ, \leq) be an ordered semigroup, then the (λ, μ) -fuzzy right (resp. left) ideals of *S* are (λ, μ) -fuzzy quasi-ideals of *S*.

Proof. Let *f* be a (λ, μ) -fuzzy right ideal of *S* and $x \in S$. First we have

$$((f*1) \cap (1*f))(x) = (f*1)(x) \wedge (1*f)(x).$$
(3.1)

If $A_x = \emptyset$, then we have (f * 1)(x) = 0 = (1 * f)(x). So $f(x) \lor \lambda \ge 0 = (f * 1)(x) \land (1 * f)(x) \land \mu$. Thus, $f \cup \lambda \supseteq (f * 1) \cap (1 * f) \cap \mu$.

If $A_x \neq \emptyset$, then

$$(f*1)(x) = \sup_{(u,v)\in A_x} (f(u) \wedge 1(v)).$$
 (3.2)

On the other hand, $f(x) \lor \lambda \ge f(u) \land 1(v) \land \mu$, for all $(u, v) \in A_x$.

Indeed, if $(u, v) \in A_x$, then $x \le uv$, thus $f(x) \lor \lambda = f(x) \lor \lambda \lor \lambda \ge (f(uv) \land \mu) \lor \lambda = (f(uv) \lor \lambda) \land (\lambda \lor \mu) \ge (f(u) \land \mu) \land \mu = f(u) \land \mu = f(u) \land 1(v) \land \mu$.

Hence, we have that $f(x) \lor \lambda \ge (\sup_{(u,v) \in A_x} (f(u) \land 1(v))) \land \mu = (f * 1)(x) \land \mu \ge (f * 1)(x) \land (1 * f)(x) \land \mu$. Thus, $f \cup \lambda \supseteq (f * 1) \cap (1 * f) \cap \mu$. Therefore, f is a (λ, μ) -fuzzy quasi-ideal of S.

Theorem 3.9. Let (S, \circ, \leq) be an ordered semigroup, then the (λ, μ) -fuzzy quasi-ideals of S are (λ, μ) -fuzzy bi-ideals of S.

Proof. Let *f* be a (λ, μ) -fuzzy quasi-ideal of *S* and $x, y, z \in S$. Then we have that

$$f(xyz) \lor \lambda \ge (f*1)(xyz) \land (1*f)(xyz) \land \mu.$$
(3.3)

From $(x, yz) \in A_{xyz}$, we have that $(f * 1)(xyz) \ge f(x) \land 1(yz) = f(x)$. From $(xy, z) \in A_{xyz}$, we have that $(1 * f)(xyz) \ge 1(xy) \land f(z) = f(z)$. Thus, $f(xyz) \lor \lambda \ge f(x) \land f(z) \land \mu$. Therefore, f is a (λ, μ) -fuzzy bi-ideal of S.

Definition 3.10 (see [5]). An ordered semigroup (S, \circ, \leq) is called regular if for all $a \in S$ there exists $x \in S$ such that $a \leq axa$.

Theorem 3.11. In a regular ordered semigroup *S*, the (λ, μ) -fuzzy quasi-ideals and the (λ, μ) -fuzzy bi-ideals coincide.

Proof. Let *f* be a (λ, μ) -fuzzy bi-ideal of *S* and $x \in S$. We need to prove that

$$f(x) \lor \lambda \ge (f * 1)(x) \land (1 * f) \land \mu.$$
(3.4)

If $A_x = \emptyset$, it is easy to verify that condition (3.4) is satisfied. Let $A_x \neq \emptyset$.

(1) If $(f * 1)(x) \land \mu \leq f(x) \lor \lambda$, then we have that $f(x) \lor \lambda \geq (f * 1)(x) \land \mu \geq (f * 1)(x) \land$ (1 * *f*)(*x*) $\land \mu$. Thus, condition (3.4) is satisfied.

(2) If $(f * 1)(x) \land \mu > f(x) \lor \lambda$, then there exists at least one pair $(z, w) \in A_x$ such that $f(z) \land 1(w) \land \mu > f(x) \lor \lambda$. That is $z, w \in S, x \le zw$ and $f(z) \land \mu > f(x) \lor \lambda$.

We will prove that $(1 * f)(x) \land \mu \leq f(x) \lor \lambda$. Then, $f(x) \lor \lambda \geq (1 * f)(x) \land \mu \geq (f * 1)(x) \land (1 * f)(x) \land \mu$, and condition (3.4) is satisfied.

For any $(u, v) \in A_x$, we need to show that $1(u) \land f(v) \land \mu \leq f(x) \lor \lambda$.

Let $(u, v) \in A_x$, then $x \le uv$ for some $u, v \in S$. Since *S* is regular, there exists $s \in S$ such that $x \le xsx$.

From $x \le xsx$, $x \le zw$ and $x \le uv$, we obtain that $x \le zwsuv$. Since f is a (λ, μ) -fuzzy bi-ideal of S, we have that

$$f(x) \lor \lambda \ge (f(zwsuv) \land \mu) \lor \lambda = (f(zwsuv) \lor \lambda) \land (\mu \lor \lambda) \ge f(z) \land f(v) \land \mu.$$
(3.5)

Note that $f(z) \land \mu > f(x) \lor \lambda$. Thus, $f(x) \lor \lambda \ge f(v) \land \mu = 1(u) \land f(v) \land \mu$.

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