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FIXED TIME IMPULSIVE DIFFERENTIAL INCLUSIONS

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Abstract. In the paper we study weak and strong invariance of differential inclusions with fixed time impulses and with state constraints.

We also investigate some properties of the solution set of impulsive system without state constraints. When the right-hand side is one sided Lipschitz we prove also the relaxation theorem and study the funnel equation of the reachable set.

Full text

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