

## A GENERAL UNIQUE COMMON FIXED POINT THEOREM FOR HYBRID PAIRS OF MAPPINGS IN METRIC SPACES

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**Abstract.** The purpose of this paper is to prove a general unique common fixed point theorem for two pairs of mappings using Hausdorff - Pompeiu metric, which generalizes, in a correct form, the results from [8] and extends Theorem 2.4 [9], for occasionally  $(f, F)$  - weakly commuting mappings.

[Full text](#)

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